

Min-Max Normalization and Example



$$v' = \frac{v - \min_A}{\max_A - \min_A} (\text{new_max}_A - \text{new_min}_A) + \text{new_min}_A$$

Min-max normalization. Suppose that the minimum and maximum values for the attribute *income* are \$12,000 and \$98,000, respectively. We would like to map *income* to the range $[0.0, 1.0]$. By min-max normalization, a value of \$73,600 for *income* is transformed to $\frac{73,600 - 12,000}{98,000 - 12,000} (1.0 - 0) + 0 = 0.716$. ■

Z-Score Normalization and Example



$$v' = \frac{v - \bar{A}}{\sigma_A}$$

z-score normalization Suppose that the mean and standard deviation of the values for the attribute *income* are \$54,000 and \$16,000, respectively. With z-score normalization, a value of \$73,600 for *income* is transformed to $\frac{73,600 - 54,000}{16,000} = 1.225$. ■

Decimal Scaling and Example



$$v' = \frac{v}{10^j}$$

Decimal scaling. Suppose that the recorded values of A range from -986 to 917 . The maximum absolute value of A is 986 . To normalize by decimal scaling, we therefore divide each value by $1,000$ (i.e., $j = 3$) so that -986 normalizes to -0.986 and 917 normalizes to 0.917 . ■

Problem



Suppose that the data for analysis includes the attribute age. The age values for the data tuples are (in increasing order)

13, 15, 16, 16, 19, 20, 20, 21, 22, 22, 25, 25, 25, 25, 30, 33, 33, 35, 35, 35, 35, 36, 40, 45, 46, 52, 70

- (a) Use min-max normalization to transform the value 35 for age onto the range $[0.0, 1.0]$.
- (b) Use z-score normalization to transform the value 35 for age, where the standard deviation of age is 12.94 years.
- (c) Use normalization by decimal scaling to transform the value 35 for age.
- (d) Comment on which method you would prefer to use for the given data, giving reasons as to why.

Problem



Use the two methods below to normalize the following group of data: 200, 300, 400, 600, 1000

- (a) min-max normalization by setting min = 0 and max = 1
- (b) z-score normalization (stdev=316.22)

Data	Min-Max Normalized Values	Z-Score Values
200	?	?
300	?	?
400	?	?
600	?	?
1000	?	?

Data Reduction



Data reduction techniques can be applied to obtain a reduced representation of the data set that is much smaller in volume, yet closely maintains the integrity of the original data.

Strategies of Data Reduction



Data Cube Aggregation

Attribute Subset Selection

Dimensionality Reduction

Numerosity Reduction

Discretization and Concept Hierarchy Generation

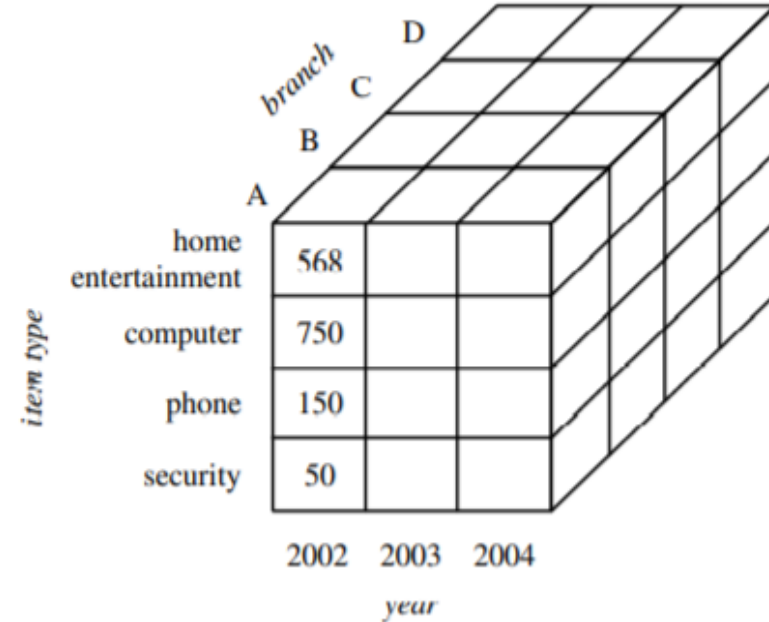
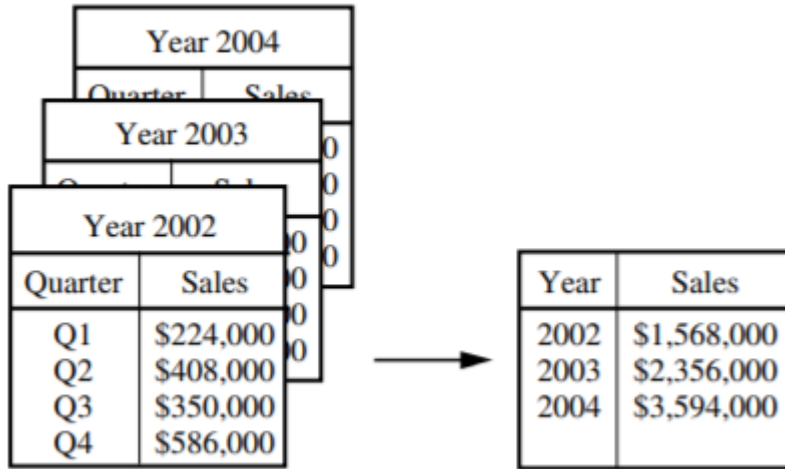
Data Cube Aggregation



Data Cube Aggregation

Aggregation operations are applied to the data in the construction of the data cube

Data Cube Aggregation : Example



Attribute Subset Selection



“where irrelevant, weakly relevant, or redundant attributes or dimensions may be detected and removed.”

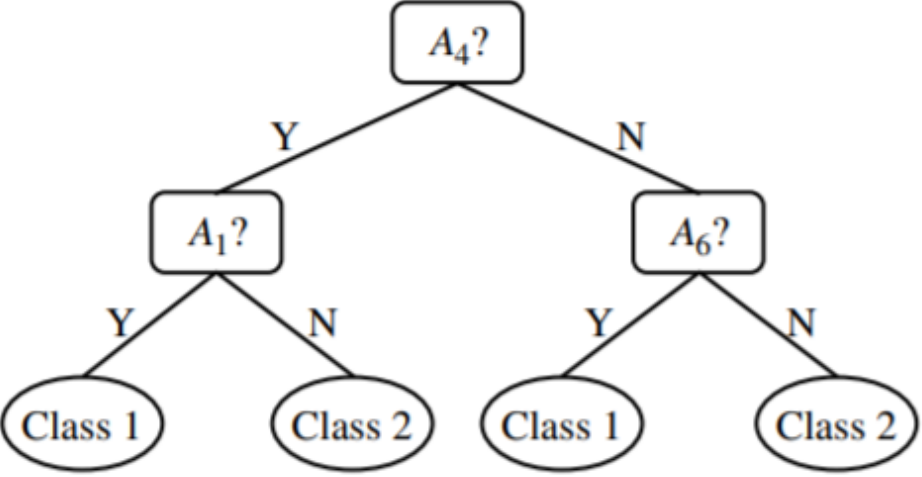
Reduces the dataset size

Minimum set of attributes

Attribute Subset Selection



1. Stepwise forward selection
2. Stepwise backward elimination
3. Combination of forward selection and backward elimination
4. Decision tree induction

Forward selection	Backward elimination	Decision tree induction
<p>Initial attribute set: $\{A_1, A_2, A_3, A_4, A_5, A_6\}$</p> <p>Initial reduced set: $\{\}$ $\Rightarrow \{A_1\}$ $\Rightarrow \{A_1, A_4\}$ \Rightarrow Reduced attribute set: $\{A_1, A_4, A_6\}$</p>	<p>Initial attribute set: $\{A_1, A_2, A_3, A_4, A_5, A_6\}$</p> <p>$\Rightarrow \{A_1, A_3, A_4, A_5, A_6\}$ $\Rightarrow \{A_1, A_4, A_5, A_6\}$ \Rightarrow Reduced attribute set: $\{A_1, A_4, A_6\}$</p>	<p>Initial attribute set: $\{A_1, A_2, A_3, A_4, A_5, A_6\}$</p>  <pre> graph TD A4["A4?"] -- Y --> A1["A1?"] A4 -- N --> A6["A6?"] A1 -- Y --> C1_1((Class 1)) A1 -- N --> C2_1((Class 2)) A6 -- Y --> C1_2((Class 1)) A6 -- N --> C2_2((Class 2)) </pre> <p>\Rightarrow Reduced attribute set: $\{A_1, A_4, A_6\}$</p>